

- 1 Let  $F$  be the function such that

$$F(z) = \frac{2z + 1}{z - 5}$$

for every possible real number  $z$ . What is the domain of  $F$ ? (Show at least one intermediate step.)

The operations involved in the formula for  $F$  are addition, subtraction, multiplication, and division. Most of these are always defined, but division by zero is undefined. Since the formula asks us to divide by  $z - 5$ , this cannot be zero. Thus:

$$\begin{aligned}z - 5 &\neq 0; \\ z &\neq 5.\end{aligned}$$

This is enough; but a fully proper answer would be either of the following:

$$\begin{aligned}\text{dom } F &= \{z \mid z \neq 5\}, \\ \text{dom } F &= (-\infty, 5) \cup (5, \infty).\end{aligned}$$

(The latter of these uses interval notation, which is probably more trouble than it's worth here, although it's often nice when you get the answer from a graph.)

- 2 Let  $f$  be the function whose graph appears in Exercise 8.4.9 of the textbook.

- a What is  $f(6)$ ?

Since  $(6, 2)$  is on the graph of  $f$ ,

$$f(6) = 2.$$

- b What is the solution to the equation  $f(x) = 3$ ?

Since  $(-3, 3)$  is on the graph of  $f$ ,  $f(-3) = 3$ ; furthermore, the *only* point  $(x, 3)$  on the graph is  $(-3, 3)$ . Therefore, the solution to the equation is simply

$$x = -3.$$