

1 Consider the line through the point $(1, 2)$ with slope 3.

a Draw a graph of this line on the number plane below.

I start at the point $(1, 2)$ and move either up 3 and right 1 or down 3 and left 1, as often as fits. This produces also the points $(2, 5)$, $(0, -1)$, and $(-1, -4)$. The graph is on the next page.

b **Extra credit:** Refer to your graph; what is its y -intercept? What is an equation for this line?

Since the line goes through

$$(0, -1),$$

that is the intercept. Since also the slope is 3, an equation for the line is

$$y = 3x - 1.$$

2 Consider the line with equation

$$2x + y = 2.$$

a What is the slope of this line? (Show what equation you solve or what numerical calculation you make.)

I solve the equation for y :

$$\begin{aligned} 2x + y &= 2; \\ y &= -2x + 2. \end{aligned}$$

Since the coefficient on x is -2 , the slope of the line is also

$$-2.$$

b What is the slope of a line perpendicular to this line?

Since the slope of the original line is -2 , the slope of the perpendicular line is

$$-\frac{1}{-2} = 1/2.$$

c Find an equation for a line that passes through $(-3, 0)$ and is perpendicular to the line above.

This line with slope $1/2$ goes through $(-3, 0)$, so its equation is

$$\begin{aligned} y &= \frac{1}{2}[x - (-3)] + 0; \\ y &= \frac{1}{2}x + \frac{3}{2}. \end{aligned}$$

