

- 1 Consider the graph of the equation

$$x^2 + y - 9 = 0$$

and answer the following questions about it. (Either show what equations you use to answer these questions or draw a graph in which the answers can clearly be seen.)

- a Is the graph symmetric with respect to the  $x$ -axis?

I change  $y$  to  $-y$ , simplify, and compare with the original:

$$\begin{aligned}x^2 + (-y) - 9 &= 0; \\x^2 - y - 9 &= 0.\end{aligned}$$

This is different from the original, so the graph is **not symmetric** with respect to the  $x$ -axis.

- b Is the graph symmetric with respect to the  $y$ -axis?

This time I change  $x$  to  $-x$ :

$$\begin{aligned}(-x)^2 + y - 9 &= 0; \\x^2 + y - 9 &= 0.\end{aligned}$$

This is the same as the original, so the graph is **symmetric** with respect to the  $y$ -axis.

- c Is the graph symmetric with respect to the origin?

This time I change both:

$$\begin{aligned}(-x)^2 + (-y) - 9 &= 0; \\x^2 - y - 9 &= 0.\end{aligned}$$

This is different from the original, so the graph is **not symmetric** with respect to the origin.

- 2 Consider the line with equation

$$2x + y = 2.$$

- a What is the slope of this line? (Show what equation you solve or what numerical calculation you make.)

I solve the equation for  $y$ :

$$\begin{aligned}2x + y &= 2; \\y &= -2x + 2.\end{aligned}$$

Since the coefficient on  $x$  is  $-2$ , the slope of the line is also

$$-2.$$

- b Find an equation for a line that passes through  $(-3, 0)$  and is perpendicular to the line above. (Show what equations you solve or what numerical calculations you make to find the constants in this equation.)

Since the slope of the original line is  $-2$ , the slope of the perpendicular line is  $-\frac{1}{-2} = 1/2$ . This line goes through  $(-3, 0)$ , so its equation is

$$\begin{aligned}y &= \frac{1}{2}[x - (-3)] + 0; \\y &= \frac{1}{2}x + \frac{3}{2}.\end{aligned}$$