

1 Let  $g$  be the function such that

$$g(x) = \frac{1}{x^2}$$

for all possible  $x$ . Is  $g$  even, odd, or neither? (Either show what calculation you make to decide this, or draw a graph that shows your answer.)

Since

$$g(-x) = \frac{1}{(-x)^2} = \frac{1}{x^2}$$

and this is the same as  $g(x)$ , it follows that  $g$  is **even**.

2 Let  $h$  be the function given by

$$h(x) = x^2 - 2x.$$

What is the average rate of change of  $h$  from 2 to 4? (Show what numerical calculation you make or what equation you solve.)

First,

$$h(2) = (2)^2 - 2(2) = 0;$$

next,

$$h(4) = (4)^2 - 2(4) = 8.$$

Therefore, the average rate of change is

$$\frac{h(4) - h(2)}{(4) - (2)} = \frac{8 - 0}{4 - 2} = \frac{8}{2} = 4.$$

3 Let  $f$  be the function shown on the screen.

a How many local minima does  $f$  have?

It has 3 local minima. (See  $(-8, -4)$ ,  $(0, 0)$ , and  $(5, 0)$  on the graph.)

b For each local minimum of  $f$ , state where it is and what it is.

One local minimum is at  $-8$ ; it is  $-4$ . Another local minimum is at  $0$ ; it is  $0$ . The last local minimum is at  $5$ ; it is also  $0$ .

c **Extra credit:** Are any of these local minima absolute? which?

Yes, the local minimum at  $-8$  is absolute; the absolute minimum of  $h$  is  $-4$ .