

1 What is 24° in radians?

a $\frac{\pi}{15} \approx 0.209$

b $\frac{1}{15} \approx 0.067$

c $\frac{2}{15} \approx 0.133$

d $\frac{2\pi}{15} \approx 0.419$

2 What is $9\pi/10$ in degrees?

a 0.005°

b 162°

c 324°

d 0.9°

3 What is the exact value of $\cos(3\pi/4)$?

a $\frac{\sqrt{2}}{2}$

b $\frac{\sqrt{3}}{2}$

c $-\frac{\sqrt{2}}{2}$

d $-\frac{\sqrt{3}}{2}$

4 What is the exact value of $\sec(\pi/3)$?

a 2

b $\frac{2\sqrt{3}}{3}$

c $\frac{\sqrt{3}}{2}$

d $\frac{1}{2}$

5 What is the exact value of $\cot(-90^\circ)$?

a 1

b -1

c undefined

d 0

6 What are the amplitude and period of the function

$$f(x) = -\frac{1}{2} \sin(2x)?$$

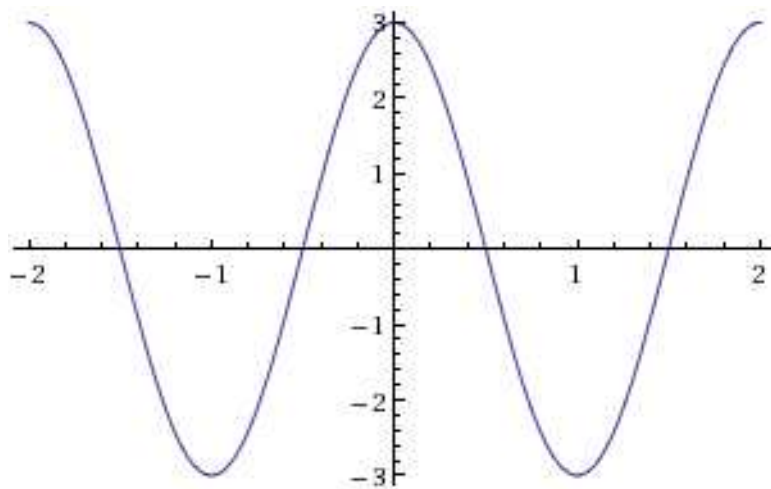
a The amplitude is $-\frac{1}{2}$, and the period is 2.

b The amplitude is 2, and the period is $\frac{1}{2}$.

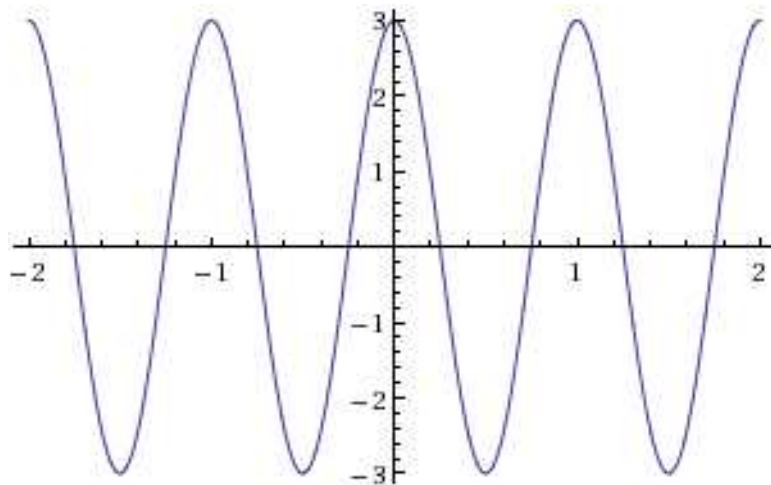
c The amplitude is $\frac{1}{2}$, and the period is π .

d The amplitude is 2π , and the period is 2.

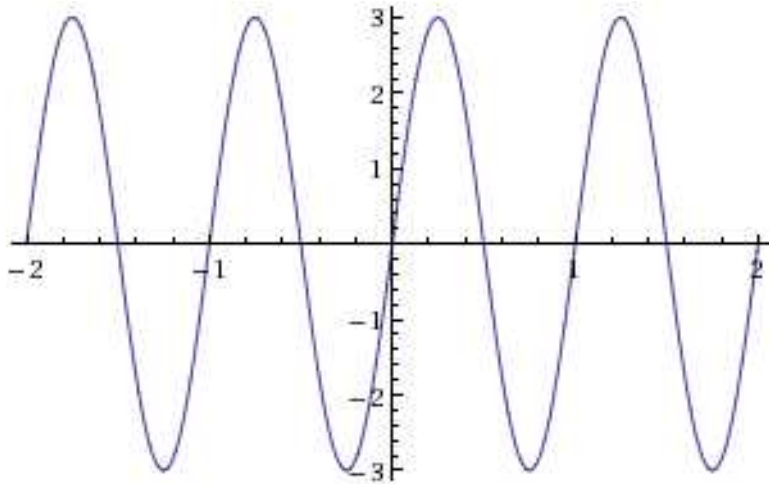
7 What is the graph of the function $f(x) = 3 \cos(\pi x)$?



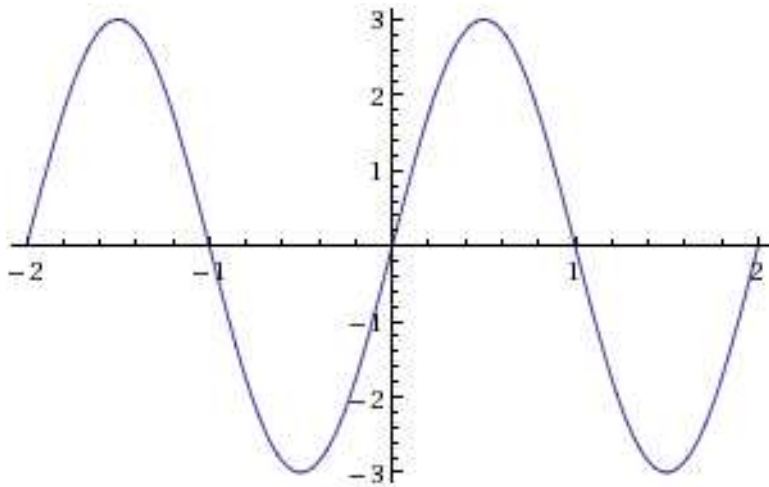
a



b



c



d

8 What is $\operatorname{arccot}(-\sqrt{3}) = \cot^{-1}(-\sqrt{3})$?

a $-\frac{\pi}{6}$

b $\frac{5\pi}{6}$

c $\frac{\pi}{6}$

d $\frac{\pi}{3}$

9 What is the exact value of $\cos 105^\circ$?

a $-\frac{\sqrt{2} + \sqrt{6}}{4} = \frac{-\sqrt{2} - \sqrt{6}}{4} = \frac{\sqrt{2 + \sqrt{3}}}{2}$

b $\frac{\sqrt{2} - \sqrt{6}}{4} = -\frac{\sqrt{2 - \sqrt{3}}}{2}$

c $\frac{\sqrt{6} - \sqrt{2}}{4} = \frac{\sqrt{2 - \sqrt{3}}}{2}$

$$d \frac{\sqrt{2} + \sqrt{6}}{4} = \frac{\sqrt{2 + \sqrt{3}}}{2}$$

10 Solve the equation $2 \cos \theta + 1 = 2$ for $0 \leq \theta < 2\pi$.

a $\theta = \frac{\pi}{3}, \frac{2\pi}{3}$

b $\theta = \frac{\pi}{3}, \frac{4\pi}{3}$

c $\theta = \frac{\pi}{3}$

d $\theta = \frac{\pi}{3}, \frac{5\pi}{3}$

11 A triangle has a side of length 3 and a side of length 4. The angle between these two sides has measure 40° . To solve this triangle, which other quantity should you calculate first?

a the measure of the angle opposite the side of length 4

b the measure of the angle opposite the side of length 3

c either of the above (it makes no difference)

d the length of the side opposite the angle of measure 40°

12 **Extra credit:** Solve the triangle in the previous exercise completely. (Show what equations you solve or what numerical calculations you make.)

13 A triangle has a side of length 5, and the angle opposite this side has measure 50° . Another side has length 2. How many triangles (up to congruence) meet this description?

a none

b one

c two

d three

14 Write $(x, y) = (-4, 4)$ in polar coordinates, using $r \geq 0$ and $0 \leq \theta < 2\pi$.

a $(r, \theta) = \left(4, \frac{5\pi}{4}\right)$

b $(r, \theta) = \left(-4\sqrt{2}, \frac{\pi}{4}\right)$

c $(r, \theta) = \left(4\sqrt{2}, \frac{3\pi}{4}\right)$

d $(r, \theta) = \left(2\sqrt{2}, \frac{7\pi}{4}\right)$

15 Write $(r, \theta) = (2, \pi/2)$ in rectangular coordinates.

a $(x, y) = (2, 0)$

b $(x, y) = (0, -2)$

c $(x, y) = (-2, 0)$

d $(x, y) = (0, 2)$

Answers

1 D, 2 B, 3 C, 4 A, 5 D, 6 C, 7 A, 8 B, 9 D, 10 D, 11 D, 13 B, 14 C, 15 D

12 Given $a = 3$, $b = 4$, and $C = 40^\circ$,

$$c = \sqrt{(3)^2 - 2(3)(4) \cos(40^\circ) + (4)^2} = \sqrt{25 - 24 \cos 40^\circ} \approx 2.57.$$

Then

$$A = \arccos \frac{(4)^2 + (\sqrt{25 - 24 \cos 40^\circ})^2 - (3)^2}{2(4)(\sqrt{25 - 24 \cos 40^\circ})} = \arccos \frac{4 - 3 \cos 40^\circ}{\sqrt{25 - 24 \cos 40^\circ}} \approx 48.6^\circ,$$

and

$$B = \arccos \frac{(3)^2 + (\sqrt{25 - 24 \cos 40^\circ})^2 - (4)^2}{2(3)(\sqrt{25 - 24 \cos 40^\circ})} = \arccos \frac{3 - 4 \cos 40^\circ}{\sqrt{25 - 24 \cos 40^\circ}} \approx 91.4^\circ.$$