

3.5.11 When dividing by a power or a root, it's easier to use a negative exponent.

$$y = \frac{1}{x^{10}} = x^{-10};$$

$$dy = d(x^{-10}) = -10x^{-11} dx;$$

$$\frac{dy}{dx} = -10x^{-11} = -\frac{10}{x^{11}}.$$

4.4.63 Similarly,

$$\frac{1}{(w^3 + 4)^5} = (w^3 + 4)^{-5};$$

$$d\frac{1}{(w^3 + 4)^5} = -5(w^3 + 4)^{-6} d(w^3 + 4) = -5(w^3 + 4)^{-6} (3w^2 dw);$$

$$\frac{d}{dw} \frac{1}{(w^3 + 4)^5} = -5(w^3 + 4)^{-6} (3w^2) = -\frac{15w^2}{(w^3 + 4)^6}.$$

4.3.39 Here I use the Product Rule:

$$f(x) = (2x + 1)(x^2 - 3x);$$

$$df(x) = (x^2 - 3x) d(2x + 1) + (2x + 1) d(x^2 - 3x) = (x^2 - 3x)(2 dx) + (2x + 1)(2x dx - 3 dx);$$

$$f'(x) = \frac{df(x)}{dx} = (x^2 - 3x)(2) + (2x + 1)(2x - 3) = 6x^2 - 10x - 3.$$

4.5.11 Differentiate, solve for  $dy$ , and divide by  $dx$ :

$$xy - 6 = 0;$$

$$d(xy - 6) = d(0);$$

$$y dx + x dy = 0;$$

$$x dy = -y dx;$$

$$dy = -\frac{y dx}{x};$$

$$\frac{dy}{dx} = -\frac{y}{x}.$$

When  $(x, y) = (2, 3)$ ,

$$\frac{dy}{dx} = -\frac{y}{x} = -\frac{3}{2}.$$