

4.6.3 To find dx/dt , I differentiate both sides, solve for dx , and divide by dt :

$$\begin{aligned}x^2 + y^2 &= 1; \\d(x^2 + y^2) &= d(1); \\2x \, dx + 2y \, dy &= 0; \\2x \, dx &= -2y \, dy; \\dx &= -\frac{y \, dy}{x}; \\\frac{dx}{dt} &= -\frac{y \, dy}{x \, dt}.\end{aligned}$$

When $x = -0.6$, $y = 0.8$, and $dy/dt = -4$,

$$\frac{dx}{dt} = -\frac{y \, dy}{x \, dt} = -\frac{0.8}{-0.6}(-4) = -\frac{16}{3}.$$