

3.1.29 If this works,

$$\lim_{x \rightarrow 1} \sqrt{5x + 4} = \sqrt{5(1) + 4} = 3.$$

It works!

3.1.53.A If this works,

$$\lim_{x \rightarrow -2} \frac{x^2 - x - 6}{x + 2} = \frac{(-2)^2 - (-2) - 6}{(-2) + 2} = \frac{0}{0}.$$

It doesn't work!

Since I got 0 on both sides of a fraction, I'll try to factor out $x - (-2) = x + 2$ from both sides first. So if this works,

$$\lim_{x \rightarrow -2} \frac{x^2 - x - 6}{x + 2} = \lim_{x \rightarrow -2} \frac{(x + 2)(x - 3)}{x + 2} = \lim_{x \rightarrow -2} (x - 3) = (-2) - 3 = -5.$$

Now it works!

3.2.11.C If this works,

$$\lim_{x \rightarrow 4} \frac{2x - 4}{(x - 4)^2} = \frac{2(4) - 4}{((4) - 4)^2} = \frac{4}{0}.$$

This doesn't quite work, but I may be able to get some kind of infinite limit.

As we approach the limit, $x \approx 4$ but $x \neq 4$:

$$\begin{aligned}x &\neq 4; \\x - 4 &\neq 0; \\(x - 4)^2 &> 0.\end{aligned}$$

Therefore,

$$\lim_{x \rightarrow 4} \frac{2x - 4}{(x - 4)^2} = \frac{4}{0^+} = \infty.$$