

3.8.13

$$\begin{aligned}
 y &= \ln(t^2); \\
 dy &= d(\ln(t^2)); \\
 &= \frac{d(t^2)}{t^2}; \\
 &= \frac{2t dt}{t^2}; \\
 \frac{dy}{dt} &= \frac{2t}{t^2} = \frac{2}{t}.
 \end{aligned}$$

Alternatively, you could simplify first:

$$\begin{aligned}
 y &= \ln(t^2) = 2 \ln t; \\
 dy &= d(2 \ln t) = 2 d(\ln t) = 2 \frac{dt}{t}; \\
 \frac{dy}{dt} &= \frac{2}{t}.
 \end{aligned}$$

3.8.75 This one is definitely easiest if you simplify first:

$$\begin{aligned}
 y &= \log_4 x + \log_4 x^2 \\
 &= \frac{\ln x}{\ln 4} + \frac{\ln x^2}{\ln 4} \\
 &= \frac{\ln x}{\ln 4} + \frac{2 \ln x}{\ln 4}; \\
 \frac{dy}{dx} &= \frac{1/x}{\ln 4} + \frac{2/x}{\ln 4} = \frac{1}{x \ln 4} + \frac{2}{x \ln 4}.
 \end{aligned}$$

3.9.21

$$\begin{aligned}
 y &= \cos^{-1}(x^2) \\
 dy &= -\frac{d(x^2)}{\sqrt{1-(x^2)^2}} \\
 &= -\frac{2x dx}{\sqrt{1-x^4}}; \\
 \frac{dy}{dx} &= -\frac{2x}{\sqrt{1-x^4}}.
 \end{aligned}$$

3.9.35

$$\begin{aligned}
 y &= \csc^{-1}(e^t); \\
 dy &= -\frac{d(e^t)}{|e^t| \sqrt{(e^t)^2 - 1}} \\
 &= -\frac{e^t dt}{e^t \sqrt{e^{2t} - 1}}; \\
 \frac{dy}{dt} &= -\frac{e^t}{e^t \sqrt{e^{2t} - 1}} = -\frac{1}{\sqrt{e^{2t} - 1}}.
 \end{aligned}$$